





Interacting with an artificial partner: modeling the role of emotional aspects

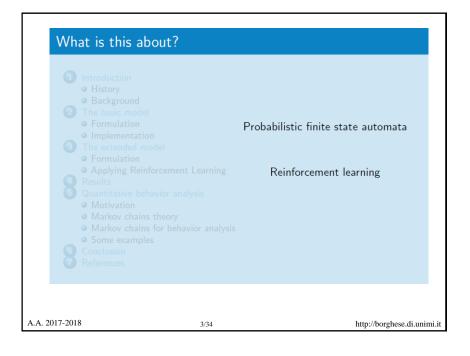
I. Cattinelli, M. Goldwurm and N.A. Borghese (2008) Biological Cybernetics, pp.254-259.

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Affective Computing What? A fairly new interd

- A fairly new interdisciplinary field, defined as computing that relates t arises from, or deliberately influences emotions [1]
- Contributions from Computer Science, Psychology, Neuroscience
- Who?
 - Research in this field "officially" started in the 1990s with Rosaline Picard and her Affective Computing Group at MIT
 - In the last years the interest toward this research area has greatly grown, as proved by a number of dedicated conferences and workshop papers and books
- How?
 - Implementation of modules for human emotion recognition, based on physiological parameters or on non-verbal communication
 - Design of systems for simulating emotional states, which can communicate emotions readable by the human user
 - Models of emotional dynamics, to explain how human emotional intelligence works and to reproduce this faculty in machines

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Affective Computing

- ... and above all: Why???
 - To get truly intelligent machines: emotions are an important part of our intellective faculties!
 - To improve human-machine interaction, making it a bit closer to human-human interaction
 - Application domains: entertainment (video games, home robots), health care, social robots

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The basic model

Let us consider a basic scenario where an artificial agent and a human partner interact.

The model for the agent's emotional dynamics is given by a four-tuple:

$$\langle S, U, P, s(0) \rangle$$

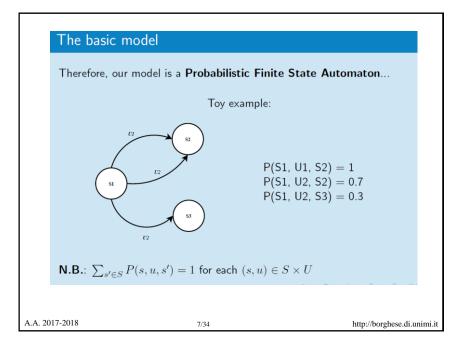
where:

- $S = \{s_1, s_2, \dots, s_N\}$ is the set of emotional states for the agent
- $U = \{u_1, u_2, \dots, u_M\}$ is the set of input (that is, the user's emotions)
- $P = \{P_0, P_1, \dots\}$ is the sequence of probabilistic transition functions:

$$P_t: S \times U \times S \rightarrow [0,1]$$
 for $t = 0,1,\ldots$

• s(0) is the initial state.

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The basic model

As we said, our model is a **Probabilistic Finite State Automaton**... whose transition probabilities may change at each step.

So, how does it work?

For each step t:

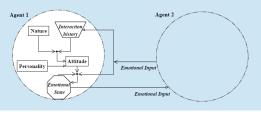
- The agent receives the user's emotional state (e.g. by analyzing her facial expression);
- ② Based on the agent's current state and input, P_t gives the probability of entering each possible next state;
- A new emotional state is chosen by the agent based on these probabilities;
- \circ P_t is (possibly) modified to get P_{t+1} ;
- **o** Go to 1.

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The basic model

We now introduce a specific terminology:

- The initial transition probability function, P_0 , is called **personality** of the agent;
- The current transition probability function, P_t , is called **attitude** of the agent;
- The criterion that drives the update of the transition probabilities is called **nature** of the agent



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The basic model

We have not mentioned, yet, how transition probabilities are being changed...

- \bullet Emotional inputs are grouped into K categories c_k (e.g. "nice" inputs)
- ullet Each category has an eligibility trace $e_t(c_k)$ associated
- ullet Each category has a set of target states $TS(c_k)$ associated
- When $e_t(c_k)$ exceeds a given threshold, the probability of entering the corresponding target states is incremented:

$$P_{t+1}(s, u, ts) = P_t(s, u, ts) + \Delta \quad \forall s \in S, u \in U, ts \in TS(c_k)$$

Target states for each category are defined by the agent's **nature**. Example: for an imitative nature, $c_k = \text{joyful inputs}$, $TS(c_k) = \{\text{JOYFUL}\}$

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Reminder: Eligibility trace

The eligibility trace in $TD(\lambda)$ algorithms keeps a history of visited states.

Here, the eligibility trace for each input category \boldsymbol{c}_k keeps a history of received inputs:

$$e_t(c_k) = \left\{ \begin{array}{ll} \alpha e_{t-1}(c_k) + h(c_k, u_j) & \text{if the current input is} \\ & \text{clustered in category } c_k \\ \alpha e_{t-1}(c_k) & \text{otherwise} \end{array} \right.$$

- \bullet α is the decay parameter;
- ullet $h(c_k,u_j)$ represents the affinity between the input and the category

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Human-robot interaction

The basic model was at first implemented in a real human-robot interaction setting.

- Robot has 4 emotional states
 - NEUTRAL, JOYFUL, SAD, ANGRY
- User gives one of 7 emotional states as an input:
 - the six basic emotions according to Ekman [2] (JOYFUL, SAD, SURPRISED, ANGRY, FEARFUL, DISGUSTED), plus the NEUTRAL state
- Input is given via facial expressions, which are captured by the robot' camera and analyzed by basic image processing techniques
 - \bullet color segmentation, border extraction, block matching... \to to get real-time processing
 - the facial expression is coded into a set of Action Units [3]
 - detected AUs are then mapped into emotions through a fuzzy-like scoring system



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Agent-agent emotional interaction

Now, let us consider two synthetic agents interacting... How do we get there?

Simple! We use two PFSA:

$$A^1 = \left\langle S, U, P^1, s(0)^1 \right\rangle$$
 and $A^2 = \left\langle S, U, P^2, s(0)^2 \right\rangle$, where:

- the set of emotional states S is the same for both A^1 and A^2 ;
- ullet the set of possible inputs, U, is coincident with the possible states, S
- the probabilistic transition functions, P_0^1 and P_0^2 , are different at start, that is the two agents have different personalities;
- the initial states $s(0)^1$ and $s(0)^2$ are different.

In brief: the state of A^1 is the input for A^2 , and vice versa.

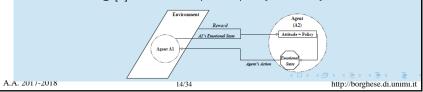
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Learning Attitudes

Adaptation to the partner may be attained through the probabilities update mechanism described above...

... or, we can assign interaction goals to one agent and apply reinforcement learning [4]

- ullet Agent A^1 acts as the environment, whose states
 - are observable by the learning agent
 - can be changed by the learning agent through its own "actions"
 - can be either goal or non-goal states
- Agent A^2 is the learning agent, and
 - receives positive reward when the environment gets to a goal state
 - has to learn a *policy* to maximize the long-term reward
- **Q-learning** [5] is used for optimal policy discovery



Learning Attitudes

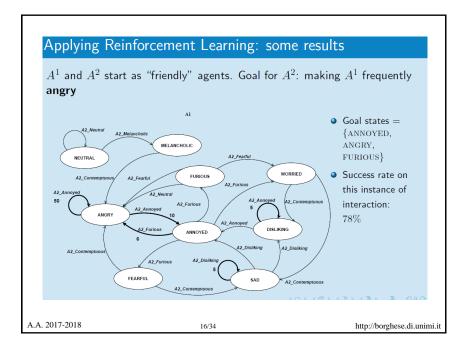
In this framework, Q(s,a) is initialized to P_0^2 .

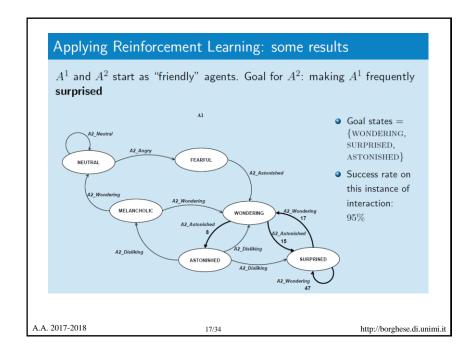
At each step t:

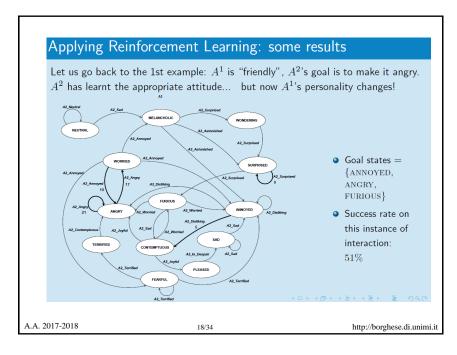
- the learning agent observes state s and takes action a according to Q(s,a): i.e., it takes action a, when seeing s, with a probability given by P_t^2 ;
- ② the agent observes the new state s' and the associated reward (= 1 only if s' is a goal state);
- **3** $Q (= P_t^2)$ is updated according to Eq. 1;
- **o** go to (1).

The policy being learned is therefore the agent's attitude.

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Quantitative behavior analysis

Problem: how can we evaluate such a model? Which quantitative measures can we derive?

Solution: Let us resort to Markov chains theory for a description of the asymptotic behavior of the system!

- Which states will be the most frequent ones?
- How long will it take to go from state i to state j?
- ...

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Markov chains [6]

Given:

- ullet a finite set of states, S;
- ullet a probability distribution $\mu^{(0)}$ over S, termed the initial distribution
- ullet a stochastic matrix P with indexes in S, called the *transition matrix*

Definition

- a **finite homogeneous Markov chain** is a sequence of random variables $\{X_n\}_{n\in\mathbb{N}}$ such that
 - for every $i \in S$, $\Pr(X_0 = i) = \mu^{(0)}(i)$
 - for every integer n>0, $i,j\in S$, and for every n-tuple i_0,i_1,\ldots,i_{n-1} , $\Pr(X_{n+1}=j|X_0=i_0,X_1=i_1,\ldots,X_{n-1}=i_{n-1},X_n=i)=\Pr(X_{n+1}=j|X_n=i)$
- for every $n \in \mathbb{N}$ and $i, j \in S$, $\Pr(X_{n+1} = j | X_n = i) = p(i, j)$

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Markov chains

Moreover, let us call $\mu^{(n)}$, for every integer n, the probability distribution of X_n . Then:

- $\bullet \ \operatorname{Pr}(X_n=j|X_0=i)=(P^n)_{ij} \qquad \quad \to \operatorname{prob. of going from } i \text{ to } j \text{ in } n \text{ steps}$
- $\bullet \ \mu_j^{(n)} = \Pr(X_n = j) = (\mu^{(0)'}P^n)_j \quad \to \text{prob. of being in } j \text{ at the } n\text{-th step}$

We are particularly interested in $\bf primitive$ Markov chains, that is chains having transition matrix P such that

$$P^k > 0$$
 for some $k \in \mathbb{N}$

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Markov chains A primitive Markov chain is: • irreducible → strongly connected transition graph • aperiodic → the greatest common divisor of the lengths of cycles is 1 Question time! • Which graph is a strongly connected one? • Which one is aperiodic?

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Properties of primitive Markov chains

1 There exists a unique **stationary distribution** π over S:

$$\pi' P = \pi'$$

where π' is a left eigenvector of P corresponding to the eigenvalue 1

2 For every $i, j \in S$

$$\lim_{n \to +\infty} (P^n)_{ij} = \lim_{n \to +\infty} \Pr(X_n = j) = \pi_j$$

that is, the limit distribution of X_n is independent from the initial state of the chain, and is coincident with the unique stationary distribution

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Properties of primitive Markov chains

The error in the approximation of $\mu^{(n)}$ towards π can be kept arbitrarily small by controlling n.

 \bullet For every $\varepsilon > 0$

$$d_{TV}(\mu^{(n)}, \pi) \le \varepsilon$$

for all $n \in \mathbb{N}$ such that

$$n \geq t \left(1 + \frac{\log_2 k - \log_2 \varepsilon - 1}{-\log_2 m(P^t)} \right)$$

where

- \bullet d_{TV} is the total variation distance between two probability distributions: $d_{TV}(\mu,\nu)=\frac{1}{2}\sum_{i\in S}|\mu_i-\nu_i|$ • t is the smallest integer such that $P^t>0$
- \bullet k is the cardinality of S
- ullet m(T) is a coefficient defined over a stochastic matrix T, such that $m(T) = \frac{1}{2} \max_{i,j \in S} \{ \sum_{l \in S} |T_{il} - T_{jl}| \}$

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Properties of primitive Markov chains - Average waiting time for first entrance

For every $j \in S$, let τ_j be the random variable defined by

$$\tau_j = \min\{n > 0 \mid X_n = j\}$$

Then, $E_i(\tau_j) = E(\tau_j \mid X_0 = i)$ is the mean waiting time for the first entrance in j starting from state i.

- \bullet $E_i(\tau_i) = 1/\pi_i$ for each $j \in S$
- **5** For $i \neq j$, the values $E_i(\tau_i)$ can be computed as well...
 - \bullet Let G(z) be the matrix of polynomials in the variable z given by G(z)=I-Pz
 - Let $r_{ij}(z)$ be the entry of indexes i,j of the adjunct of G(z): $r_{ij}(z) = (-1)^{i+j} \det(G_{ji}(z))$ where $G_{ji}(z)$ is the matrix obtained from G(z) by deleting the j-th row and the i-th column
 - $E_i(\tau_j) = \frac{r'_{ij}r_{jj} r_{ij}r'_{jj}}{r^2_{jj}}$, where $r_{ij} = r_{ij}(1)$, $r_{jj} = r_{jj}(1)$, $r'_{ij} = r'_{ij}(1)$ and $r'_{ij} = r'_{ji}(1)$

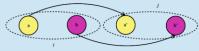
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Markov chains and the interaction model

How can all this be related to our model? Markov chains have no inputs!

Yes, but...

- \bullet We can build one transition matrix, M, for the whole interaction system
- M(i,j) gives the probability to go from state i=(a,b) to state j=(a',b'), with a,a' emotional states for agent A^1 , and b,b' states for A^2



• $M(i,j) = P^1(a,b,a') \times P^2(b,a',b')$

... and so now we have all the ingredients for a Markov chain!

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Markov chains and the interaction model

We have seen that primitive Markov chains have interesting properties, so: is our ${\cal M}$ primitive?

No! Because it is generally not irreducible...

Solution: let us reduce it!

- \bullet M not irreducible \to the transition graph has more than one strongly connected component
- Some of them will be essential components: once entered, they will never be left

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Quantitative behavior analysis – Limit probability of states

Let us consider again the previously shown interaction systems:

- $\ \, \textbf{0} \,\, A^1$ friendly, A^2 acquired a policy for making the partner angry most of the time (fig.)
 - M_{red} is composed of 15 states
 - ullet the most probable states according to π are
 - (ANGRY, ANNOYED), with p = 0.5148
 - (ANNOYED, FURIOUS), with p = 0.1548
 - (SAD, DISLIKING), with p = 0.0973
- ② A^1 friendly, A^2 acquired a policy for making the partner surprised most of the time (fig.)
 - M_{red} is composed of 10 states
 - ullet the most probable states according to π are
 - (SURPRISED, WONDERING), with p = 0.6286
 - (WONDERING, ASTONISHED), with p = 0.2292
 - (ASTONISHED, DISLIKING), with p = 0.0917

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Quantitative behavior analysis – Limit probability of states

What does this analysis tell us?

- Probability values provided by the stationary distribution are rather close to the frequencies observed in the experiments
 - the stationary distribution is a suitable descriptor of the actual behavior of the systems even after a limited amount of steps
 - \bullet the error in approximation is less than 0.001 just after 38 and 27 steps, respectively (see Prop. 3)
- The reinforcement learning process was effective
 - ullet the goal states defined for A^1 are among the most probable states of the system in each of the considered examples

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Quantitative behavior analysis – Mean entrance times

We can define a set of *starting states*, SS, and a set of *ending states*, ES, and use Prop. 4–5 to compute the mean entrance times for going from states in SS to states in ES.

Natural choice in a learning scenario: ES coincident with goal states...

- - $ES = \{(a, b) \mid a = \{\text{ANNOYED}, \text{ANGRY}, \text{FURIOUS}\}, b \in S\}$
 - $SS = \{(MELANCHOLIC, CONTEMPTUOUS)\}$
 - \bullet a minimum of 5.91 and a maximum of 213.10 steps, on average, for going from states in SS to states in ES (mean 77.98)
- $\ \, \textbf{②} \,\, A^1$ friendly, A^2 acquired a policy for making the partner surprised most of the time
 - $ES = \{(a, b) \mid a = \{\text{Wondering, surprised, astonished}\}, b \in S\}$
 - $SS = \{(NEUTRAL, ANGRY)\}$
 - a minimum of 3.86 and a maximum of 12.43 steps, on average, for going from states in SS to states in ES (mean 7.07)

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Natural choice in a learning scenario: ES coincident with goal states...

- $\ \ \, {\bf A}^1$ friendly, A^2 acquired a policy for making the partner angry most of the time
 - $ES = \{(a, b) \mid a = \{\text{Annoyed, angry, furious}\}, b \in S\}$
 - $SS = \{ (MELANCHOLIC, CONTEMPTUOUS) \}$
 - a minimum of 5.91 and a maximum of 213.10 steps, on average, for going from states in SS to states in ES (mean 77.98)
- $\ \, \textbf{@} \,\, A^1$ friendly, A^2 acquired a policy for making the partner surprised most of the time
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Quantitative behavior analysis – Mean entrance times

What does this analysis tell us?

- \bullet In the second example, the learned policy is particularly effective in driving A^1 's behavior to the given goals
 - just 7 steps are required, on average, to reach a goal state!
- In the first example, the policy is less effective, meaning that about 78 steps are required, on average, to reach a goal state...
 - ... however this is mainly due to two particular end states that have very low entrance probabilities
 - \bullet the other three goal states can be reached within $30~\mathrm{steps}$

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Summing up

We proposed an emotional interaction model:

- for a human-robot, or for an agent-agent interactions scenario
- having a probabilistic and time-varying nature, leading to more life-like interactions
- capable of adaptation to the interlocutor, either by the probabilities update mechanism or by autonomous learning
- with a basic structure that can easily be extended (adding/modifying states, inputs, personalities, ...)
- which can be employed, for instance, as a basis for emotional agents in video games, or in social robotics

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